

# Reaction kinetics modelling

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## Recommended special courses of Tamás Turányi

### **Chemistry and Physics of Flames** (in English)

- combustion chemistry
- experimental methods for the investigation of combustion reactions
- experimental determination of gas-phase rate coefficients
- physics of flame spread

### **Analysis of Kinetic Reaction Mechanisms** (in English)

- reaction kinetics modelling
- sensitivity analysis
- uncertainty analysis
- time scale analysis
- mechanism reduction

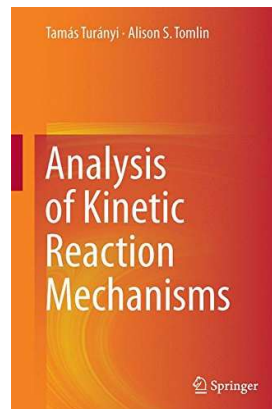
## Analysis of kinetic reaction mechanisms – the book

Tamás Turányi and Alison S. Tomlin:

Analysis of kinetic reaction mechanisms

Springer, 2014

(with 1025 references)



Web page:

<http://garfield.chem.elte.hu/Turanyi/KineticReactionMechanisms.html>

- table of contents
- download the chapters
- references
- typos found

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## Practical applications of reaction kinetics

- **modelling atmospheric chemical processes**
  - forecast of air pollution (weather forecast is needed!)
  - determination of emission limits
- **modelling of ignition and combustion**
  - modelling power stations, furnaces, engines
  - improving efficiency
  - elaboration of methods for the decrease of pollutant emission
- **process engineering; modelling of chemical engineering processes**
  - considering efficiency and the aspects of environment protection
- **systems biology: modelling biochemical processes within living organisms**
  - metabolic networks (e.g. medical drug decomposition in the body)
  - molecular signal transfer
  - modelling the cell cycle
- **non-chemical models using reaction kinetic formalism**
  - predator-prey models
  - description of ecological systems

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### Detailed reaction mechanisms: many reaction steps and many parameters

|                        |                      |
|------------------------|----------------------|
| hydrogen combustion    | 30 reaction steps    |
| natural gas combustion | 300 reaction steps   |
| petrol combustion      | 3000 reaction steps  |
| Diesel oil combustion  | 15000 reaction steps |

This is a skeleton 12-step hydrogen combustion mechanism:

|    |                                                                                  |                |
|----|----------------------------------------------------------------------------------|----------------|
| 1  | $\text{H}_2 + \text{O}_2 \rightarrow \cdot\text{H} + \cdot\text{HO}_2$           | $k_1(T)$       |
| 2  | $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$          | $k_2(T)$       |
| 3  | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$     | $k_3(T)$       |
| 4  | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{OH} + \cdot\text{H}$          | $k_4(T)$       |
| 5  | $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$  | $k_5(T, p)$    |
| 6  | $\cdot\text{H} \rightarrow \text{wall}$                                          | $k_6(T)$       |
| 7  | $\cdot\text{O} \rightarrow \text{wall}$                                          | $k_7(T)$       |
| 8  | $\cdot\text{OH} \rightarrow \text{wall}$                                         | $k_8(T)$       |
| 9  | $\cdot\text{HO}_2 + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}_2$ | $k_9(T)$       |
| 10 | $2 \cdot\text{HO}_2 \rightarrow \text{H}_2\text{O}_2 + \text{O}_2$               | $k_{10}(T)$    |
| 11 | $\text{H}_2\text{O}_2 + \text{M} \rightarrow 2 \cdot\text{OH} + \text{M}$        | $k_{11}(T, p)$ |
| 12 | $\cdot\text{HO}_2 \rightarrow \text{wall}$                                       | $k_{12}(T)$    |

$k(T, p)$

temperature-dependence: 3-parameter Arrhenius-equation  
pressure-dependence: several more parameters

Further parameters to each species: thermodynamical data, diffusion coefficients, viscosity

### Equivalence ratio

#### fuel lean combustion



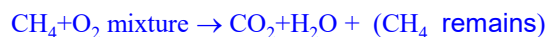
$$\varphi < 1; \lambda > 1$$

#### stoichiometric combustion



$$\varphi = 1; \lambda = 1$$

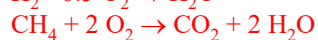
#### fuel rich combustion



$$\varphi > 1; \lambda < 1$$

In fact, no methane remains, because  
at high temperature methane decomposes  
to hydrogen and olefins!

#### Stoichiometric ratios:



$$\varphi = \frac{n_{\text{fuel}}/n_{\text{oxidizer}}}{(n_{\text{fuel}}/n_{\text{oxidizer}})_{\text{stoichiometric}}}$$

$\lambda$ : air equivalence ratio (see „ $\lambda$  sensor”)

$\varphi$ : fuel equivalence ratio  $\varphi = 1/\lambda$

## Simulation of spatially homogeneous systems

calculation of concentration changes  
(solution of the kinetic system of differential equations) :

$$\frac{d\mathbf{Y}}{dt} = \mathbf{f}(\mathbf{Y}, \mathbf{p}) \quad \mathbf{Y}(t_0) = \mathbf{Y}_0$$

calculation of temperature changes in an adiabatic system:

$$C_p \frac{dT}{dt} = \sum_{i=1}^{N_R} \Delta_r H_i^\ominus r_i \quad T(t_0) = T_0$$

↑ heat capacity of the mixture
rate of reaction step  $i$ 
↑ standard reaction enthalpy of reaction step  $i$

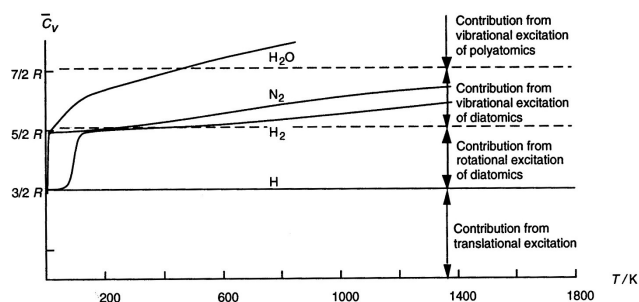
## Temperature dependence of thermodynamic data

NASA polynomials

$$\frac{H^\ominus}{RT} = a_1 + \frac{a_2}{2} T + \frac{a_3}{3} T^2 + \frac{a_4}{4} T^3 + \frac{a_5}{5} T^4 + \frac{a_6}{T}$$

$$\frac{C_p}{R} = a_1 + a_2 T + a_3 T^2 + a_4 T^3 + a_5 T^4$$

$$\frac{S^\ominus}{R} = a_1 \ln T + a_2 T + \frac{a_3}{2} T^2 + \frac{a_4}{3} T^3 + \frac{a_5}{4} T^4 + a_7$$



## Temperature dependence of rate coefficient $k$

Described by the Arrhenius equation:

$$k = A \exp\left(-\frac{E_a}{RT}\right) \qquad \ln k = \ln A - \frac{E_a}{RT}$$

A      preexponential factor  
E<sub>a</sub>    activation energy

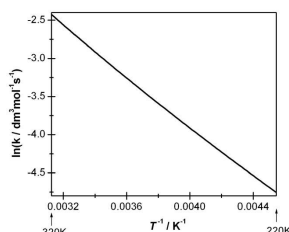
If the rate coefficient  $k$  is measured at several  $T$  temperatures and

**ln  $k$  is plotted as a function of  $1/T$**

the data fit to a line, if the (original) Arrhenius equation is valid

slope is  $m = -E_a/R$        $\Rightarrow$  determination of  $E_a$

Arrhenius plot:

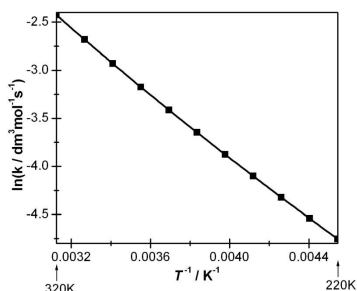


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## Example: reaction $\text{CH}_4 + \text{OH} \rightarrow \text{CH}_3 + \text{H}_2\text{O}$

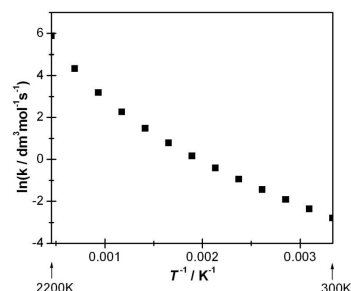
- the most important methane consuming reaction step in the troposphere
- one of the most important steps at methane combustion

Arrhenius plot between 220 K (– 53 °C )  
and 320 K (+ 47 °C)



the Arrhenius equation is usually  
very accurate in a small  
(few times 10 K) temperature range.  
(solution phase and atmospheric chemistry)

Arrhenius plot between 300 K (27 °C)  
and 2200 K (≈1930 °C)

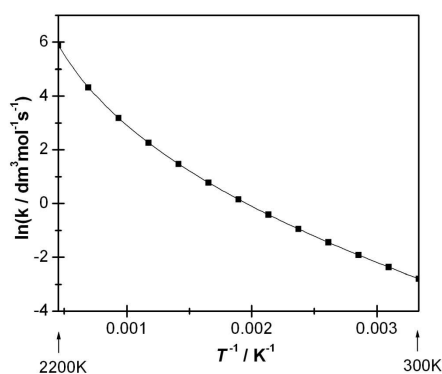


the original Arrhenius equation  
is usually not applicable in a wide  
temperature range  
(combustion and pyrolytic systems)

## Temperature dependence of the rate coefficient 2

$$k = BT^n e^{\frac{C}{RT}}$$

extended Arrhenius equation



Important!

If  $n \neq 0$  then  $A \neq B$  and  $E_a \neq C$

General definition of activation energy:

$$E_a = -R \frac{\partial \ln k}{\partial (1/T)}$$

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## Pressure dependence of the rate coefficients 1 unimolecular decomposition

decomposition or isomerization of a species



A reactant

P product

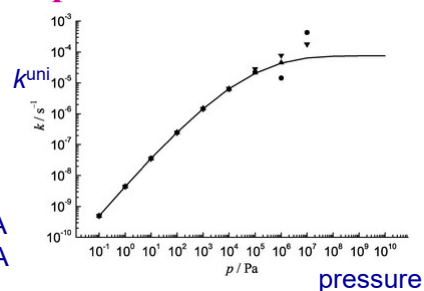
M colliding partner for energy transfer

low pressure

2<sup>nd</sup> order decay of A

high pressure

1<sup>st</sup> order decay of A



„pseudo first order” rate coefficient:

high pressure limit:

$$k_{\text{uni}} = k_{\infty}$$

low pressure limit:

$$k_{\text{uni}} = k_0 [M]$$

The temperature dependences of  $k_0$  and  $k_{\infty}$  are described independently by extended Arrhenius equations:

$$k_0 = A_0 T^{n_0} \exp\left(\frac{-E_0}{RT}\right)$$

$$k_{\infty} = A_{\infty} T^{n_{\infty}} \exp\left(\frac{-E_{\infty}}{RT}\right)$$

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### Lindemann – Hinshelwood model



high pressure:  $[M] \rightarrow \infty$        $k_{\text{uni}} \approx \frac{k_3 k_1}{k_2}$        $k_{\infty} = \frac{k_3 k_1}{k_2}$

low pressure:  $[M] \approx 0$        $k_{\text{uni}} \approx k_1 [M]$        $k_0 = k_1$

unimolecular decomposition rates:

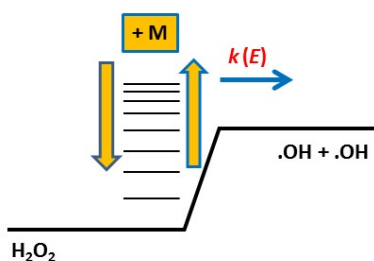
$k^{\text{uni}}$  „pseudo first order” rate coefficient ( $\text{s}^{-1}$ )  
 $k_{\infty}$  high pressure limit (first order) rate coefficient ( $\text{s}^{-1}$ )  
 $k_0$  low pressure limit (second order) rate coefficient ( $\text{mol}^{-1} \text{dm}^3 \text{s}^{-1}$ )

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### Refined Lindemann – Hinshelwood model of unimolecular reactions



- instead of assuming a single excited species,  $\text{H}_2\text{O}_2^*$  exists in a range of different rovibrationally excited states.
- the rate of the decomposition step increases with the increasing rovibrational energy of  $\text{H}_2\text{O}_2^*$



low pressure:

- the rate limiting is the collision with M
- the overall decomposition rate is proportional with pressure

high pressure:

- the rate limiting is the decomposition of  $\text{H}_2\text{O}_2^*$
- the overall decomposition rate is independent of pressure



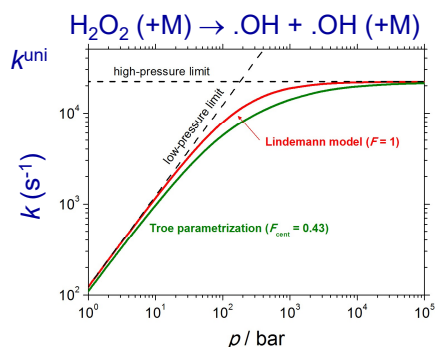
2<sup>nd</sup> order at low pressure, 1<sup>st</sup> order at high pressure<sup>14</sup>

## Unimolecular decomposition: calculation of the rate coefficient at an intermediate pressure

$$k = k_{\infty} \left( \frac{P_r}{1 + P_r} \right) F$$

$$P_r = \frac{k_0 [M]}{k_{\infty}}$$

$P_r$  reduced pressure  
 $F$  controls the shape of the  $k(p)$  curve



in the Lindemann model  $F = 1$

$F$  can be defined as a function of pressure and temperature  
 (e.g. using Troe parameterization):

$$\log F = \log F_{\text{cent}} \left[ 1 + \left[ \frac{\log P_r + c}{n - d(\log P_r + c)} \right]^2 \right]^{-1}$$

$$\begin{aligned} c &= -0.4 - 0.67 \log F_{\text{cent}} \\ n &= -0.75 - 1.271 \log F_{\text{cent}} \\ d &= 0.14 \end{aligned}$$

$$F_{\text{cent}} = (1 - \alpha) \exp\left(-\frac{T}{T^{***}}\right) + \alpha \exp\left(-\frac{T}{T^*}\right) + \exp\left(-\frac{T^{**}}{T}\right) \quad 15$$

## Collision efficiency parameters

**M** any species present in the mixture  
 BUT some species are more effective colliders

**good collider:** removes much energy from the excited species in each collision

Which are the good colliders?

- species with similar energy levels to those of the excited species
- large molecules with many energy levels

**poor collider:** e.g. noble gases:  
 no rotational or vibrational energy levels  
 only the translational mode can be excited

calculation of the effective concentration of M:

$m_i$  collision efficiency parameter

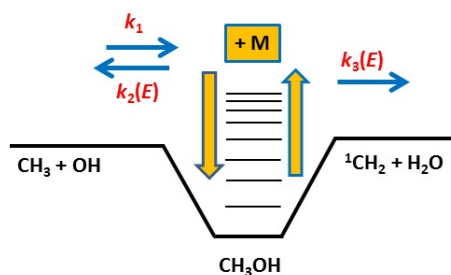
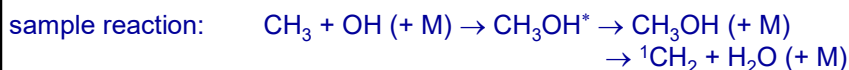
$$[M] = \sum_i m_{y_i} [Y_i]$$

calculation for reaction  $\text{H}_2\text{O}_2 (+\text{M}) \rightarrow \cdot\text{OH} + \cdot\text{OH} (+\text{M})$ :

$$[M] = 5[\text{H}_2\text{O}] + 5.13[\text{H}_2\text{O}_2] + 0.8[\text{O}_2] + 2.47[\text{H}_2] + 1.87[\text{CO}] + 1.07[\text{CO}_2] + 0.67[\text{Ar}] + 0.43[\text{He}] + [\text{all others}]$$



## Pressure dependence of the rate coefficients 2 complex-forming bimolecular reactions



low pressure:  
mainly  $\text{CH}_3\text{OH}^*$  decomposition to  
 ${}^1\text{CH}_2 + \text{H}_2\text{O}$   
( ${}^1\text{CH}_2$  = singlet  $\text{CH}_2$  =  
electronically excited  $\text{CH}_2$ )

high pressure:  
mainly  $\text{CH}_3\text{OH}^*$  stabilization,  
giving  $\text{CH}_3\text{OH}$

$\text{CH}_3 + \text{OH} \rightarrow \text{CH}_3\text{OH}$  3<sup>rd</sup> order at low pressure, 2<sup>nd</sup> order at high pressure

$\text{CH}_3 + \text{OH} \rightarrow {}^1\text{CH}_2 + \text{H}_2\text{O}$  3<sup>rd</sup> order at low pressure, 2<sup>nd</sup> order at high pressure

## Formation of the stabilization product

$$k^{\text{bi}} = k_{\infty} \left( \frac{P_r}{1 + P_r} \right) F$$

$$P_r = \frac{k_0 [\text{M}]}{k_{\infty}}$$

$P_r$  reduced pressure

$F$  controls the shape of the  
 $k(p)$  curve

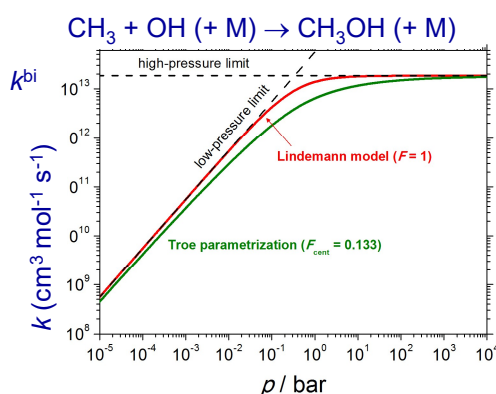
in the Lindemann model  $F = 1$

$F(p, T)$  can be defined by e.g. Troe parameterization

$k^{\text{bi}}$  „pseudo second order” rate coefficient

at low pressure:  $k^{\text{bi}} = k_0 [\text{M}]$

at high pressure:  $k^{\text{bi}} = k_{\infty}$



## Formation of the decomposition products

$$k^{\text{tri}} = k_0 \left( \frac{1}{1 + P_r} \right) F$$

$$P_r = \frac{k_0 [M]}{k_\infty}$$

$P_r$  reduced pressure

$F$  controls the shape of the  $k(p)$  curve

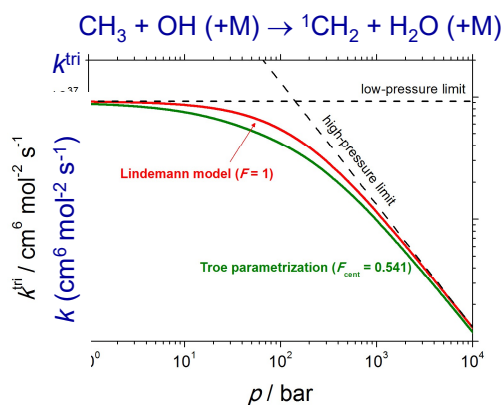
in the Lindemann model  $F = 1$

$F(p, T)$  can be defined by e.g. Troe parameterization

$k^{\text{tri}}$  „pseudo third order” rate coefficient

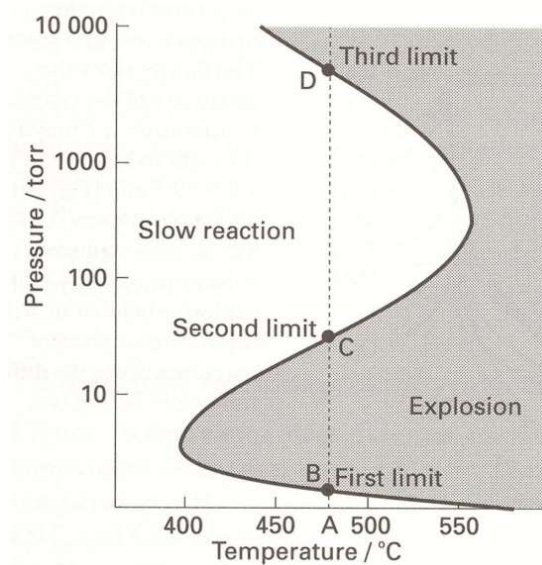
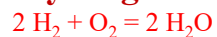
at low pressure:  $k^{\text{tri}} = k_0$

at high pressure:  $k^{\text{tri}} = k_\infty / [M]$



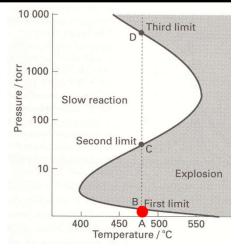
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## Explosion of a hydrogen-oxygen mixture



|    |                                                                                  |                    |
|----|----------------------------------------------------------------------------------|--------------------|
| 1  | $\text{H}_2 + \text{O}_2 \rightarrow \cdot\text{H} + \cdot\text{HO}_2$           | chain initiation   |
| 2  | $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$          | chain branching    |
| 3  | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$     | chain continuation |
| 4  | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{OH} + \cdot\text{H}$          | chain branching    |
| 5  | $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$  | chain termination* |
| 6  | $\cdot\text{H} \rightarrow \text{wall}$                                          | chain termination  |
| 7  | $\cdot\text{O} \rightarrow \text{wall}$                                          | chain termination  |
| 8  | $\cdot\text{OH} \rightarrow \text{wall}$                                         | chain termination  |
| 9  | $\cdot\text{HO}_2 + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}_2$ | chain initiation*  |
| 10 | $2 \cdot\text{HO}_2 \rightarrow \text{H}_2\text{O}_2 + \text{O}_2$               | chain termination  |
| 11 | $\text{H}_2\text{O}_2 + \text{M} \rightarrow 2 \cdot\text{OH} + \text{M}$        | chain initiation   |
| 12 | $\cdot\text{HO}_2 \rightarrow \text{wall}$                                       | chain termination  |

|    |                                                                                  |                    |
|----|----------------------------------------------------------------------------------|--------------------|
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| 3  | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$     | chain continuation |
| 4  | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{OH} + \cdot\text{H}$          | chain branching    |
| 5  | $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$  | chain termination* |
| 6  | $\cdot\text{H} \rightarrow \text{wall}$                                          | chain termination  |
| 7  | $\cdot\text{O} \rightarrow \text{wall}$                                          | chain termination  |
| 8  | $\cdot\text{OH} \rightarrow \text{wall}$                                         | chain termination  |
| 9  | $\cdot\text{HO}_2 + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}_2$ | chain initiation*  |
| 10 | $2 \cdot\text{HO}_2 \rightarrow \text{H}_2\text{O}_2 + \text{O}_2$               | chain termination  |
| 11 | $\text{H}_2\text{O}_2 + \text{M} \rightarrow 2 \cdot\text{OH} + \text{M}$        | chain initiation   |
| 12 | $\cdot\text{HO}_2 \rightarrow \text{wall}$                                       | chain termination  |



**below the 1<sup>st</sup> explosion limit:**

chain termination reactions 6, 7, 8 remove the radicals  
(radical loss on the wall)

**→ no explosion**

|    |                                                                                  |                    |
|----|----------------------------------------------------------------------------------|--------------------|
| 1  | $\text{H}_2 + \text{O}_2 \rightarrow \cdot\text{H} + \cdot\text{HO}_2$           | chain initiation   |
| 2  | $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$          | chain branching    |
| 3  | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$     | chain continuation |
| 4  | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{OH} + \cdot\text{H}$          | chain branching    |
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| 8  | $\cdot\text{OH} \rightarrow \text{wall}$                                         | chain termination  |
| 9  | $\cdot\text{HO}_2 + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}_2$ | chain initiation*  |
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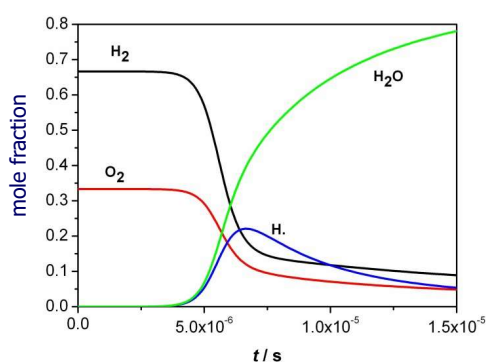
**between explosion limits 1 and 2:**

2-3-4 chain branching steps

|   |                                                                                                                             |
|---|-----------------------------------------------------------------------------------------------------------------------------|
| 2 | $\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$                                                          |
| 3 | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$                                                |
| 4 | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{H} + \cdot\text{OH}$                                                     |
| 3 | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$                                                |
| + |                                                                                                                             |
|   | $\cdot\text{H} + \text{O}_2 + 3 \text{H}_2 \rightarrow 3 \cdot\text{H} + 2 \text{H}_2\text{O} \rightarrow \text{explosion}$ |

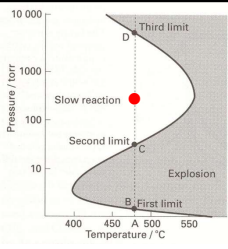
  
  

### Hydrogen-oxygen explosion between limits 1 and 2



H atom is a very reactive intermediate  
 its concentration first increases quickly + starts to decay  
 when the concentrations of  $\text{H}_2$  and  $\text{O}_2$  decreases  
 concentration of  $\text{H}_2\text{O}$ : saturation curve

|    |                                                                                  |                    |
|----|----------------------------------------------------------------------------------|--------------------|
| 1  | $\text{H}_2 + \text{O}_2 \rightarrow \cdot\text{H} + \cdot\text{HO}_2$           | chain initiation   |
| 2  | $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$          | chain branching    |
| 3  | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$     | chain continuation |
| 4  | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{OH} + \cdot\text{H}$          | chain branching    |
| 5  | $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$  | chain termination* |
| 6  | $\cdot\text{H} \rightarrow \text{wall}$                                          | chain termination  |
| 7  | $\cdot\text{O} \rightarrow \text{wall}$                                          | chain termination  |
| 8  | $\cdot\text{OH} \rightarrow \text{wall}$                                         | chain termination  |
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| 11 | $\text{H}_2\text{O}_2 + \text{M} \rightarrow 2 \cdot\text{OH} + \text{M}$        | chain initiation   |
| 12 | $\cdot\text{HO}_2 \rightarrow \text{wall}$                                       | chain termination  |



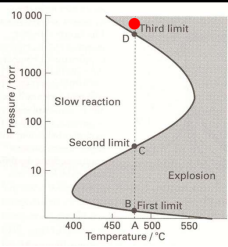
**between explosion limits 2 and 3:**

|    |                                                                                 |                    |
|----|---------------------------------------------------------------------------------|--------------------|
| 5  | $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$ | chain termination* |
| 12 | $\cdot\text{HO}_2 \rightarrow \text{wall}$                                      | chain termination  |

**→ no explosion**

M any species present  
at the hydrogen/air explosion it is mainly  $\text{N}_2$   $\text{O}_2$   $\text{H}_2$   
but can be any other species (e.g.  $\cdot\text{H}$   $\cdot\text{HO}_2$   $\cdot\text{OH}$ )

|    |                                                                                  |                    |
|----|----------------------------------------------------------------------------------|--------------------|
| 1  | $\text{H}_2 + \text{O}_2 \rightarrow \cdot\text{H} + \cdot\text{HO}_2$           | chain initiation   |
| 2  | $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$          | chain branching    |
| 3  | $\cdot\text{OH} + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}$     | chain continuation |
| 4  | $\cdot\text{O} + \text{H}_2 \rightarrow \cdot\text{OH} + \cdot\text{H}$          | chain branching    |
| 5  | $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$  | chain termination* |
| 6  | $\cdot\text{H} \rightarrow \text{wall}$                                          | chain termination  |
| 7  | $\cdot\text{O} \rightarrow \text{wall}$                                          | chain termination  |
| 8  | $\cdot\text{OH} \rightarrow \text{wall}$                                         | chain termination  |
| 9  | $\cdot\text{HO}_2 + \text{H}_2 \rightarrow \cdot\text{H} + \text{H}_2\text{O}_2$ | chain initiation*  |
| 10 | $2 \cdot\text{HO}_2 \rightarrow \text{H}_2\text{O}_2 + \text{O}_2$               | chain termination  |
| 11 | $\text{H}_2\text{O}_2 + \text{M} \rightarrow 2 \cdot\text{OH} + \text{M}$        | chain initiation   |
| 12 | $\cdot\text{HO}_2 \rightarrow \text{wall}$                                       | chain termination  |

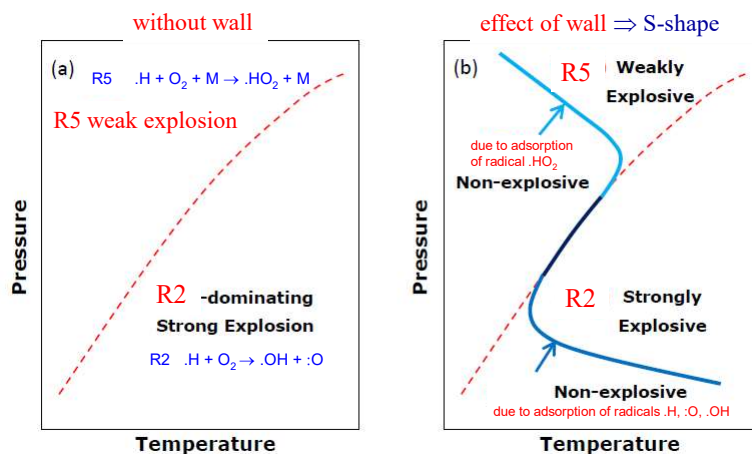


**above explosion limit 3**

- high pressure  $\Rightarrow$  reaction step 5 produces much  $\cdot\text{HO}_2$
- reaction steps 9 and 10 convert  $\cdot\text{HO}_2$  to  $\text{H}_2\text{O}_2$
- at high pressure the decomposition of  $\text{H}_2\text{O}_2$  is fast (reaction 11) and it produces highly reactive OH radicals

**→ explosion**

## Effect of the heterogeneous reactions 2



The dashed line corresponds to pressure where  $[M] = 2 k_2/k_5$   
 (R2  $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$ ) R5  $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$

The wall reactions result in the non-explosive regions!

lower non-explosive region (below limit 1):

adsorption of radicals  $\text{H}, \cdot\text{O}, \cdot\text{OH}$

upper non-explosive region (between limits 2 and 3): adsorption of radical  $\cdot\text{HO}_2$

## the key of explosion / no explosion behaviour the $\text{HO}_2$ reaction system

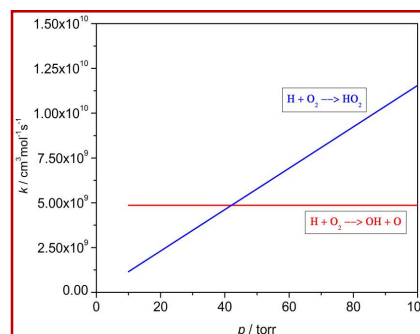
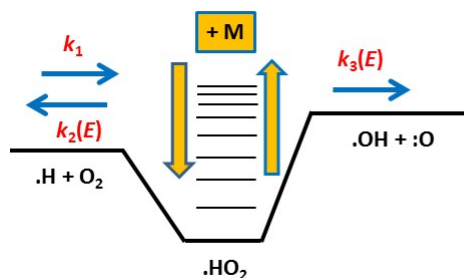
at temperature 650 K

below about 40 torr  $\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{OH} + \cdot\text{O}$

$\rightarrow$  explosion

above about 40 torr  $\cdot\text{H} + \text{O}_2 + \text{M} \rightarrow \cdot\text{HO}_2 + \text{M}$

$\rightarrow$  NO explosion



$\cdot\text{H} + \text{O}_2 \rightarrow \cdot\text{HO}_2^*$

low pressure:  $\cdot\text{HO}_2^* \rightarrow \cdot\text{H} + \text{O}_2$  or  $\cdot\text{HO}_2^* \rightarrow \cdot\text{OH} + \cdot\text{O}$

$\rightarrow$  explosion

high pressure:  $\cdot\text{HO}_2^* \rightarrow \cdot\text{HO}_2$  (stabilization)

$\rightarrow$  NO explosion

## Computer codes for the study of complex reaction systems

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### Reaction kinetics simulation codes

WINPP/XPP Windows simulation code

solving systems of ODEs, DAEs and PDEs.

The user has to provide the rate equations  $\Rightarrow$  applicable for small systems only

<http://www.math.pitt.edu/~bard/classes/wppdoc/readme.htm>

KPP: Kinetic Preprocessor <http://people.cs.vt.edu/~asandu/Software/Kpp/>

production of the kinetic ODE from the reaction mechanism

numerical solution of stiff ODEs; sparse matrix routines

V. Damian, A. Sandu, M. Damian, F. Potra, G. R. Carmichael:

The Kinetic PreProcessor KPP - A software environment for solving chemical kinetics.

*Comp. Chem. Eng.* **26**, 1567-1579 (2002)

SUNDIALS: SUite of Nonlinear and Differential/ALgebraic equation Solvers

<https://computation.llnl.gov/casc/sundials/main.html>

MATLAB interface to the following solvers:

CVODE solves initial value problems for ordinary differential equation (ODE) systems

CVODES solves ODE systems and includes sensitivity analysis capabilities

ARKODE solves initial value ODE problems with additive Runge-Kutta methods

IDA solves initial value problems for differential-algebraic equation (DAE) systems

IDAS solves DAE systems and includes sensitivity analysis capabilities

KINSOL solves nonlinear algebraic systems.

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## CHEMKIN

Developed at the SANDIA National Laboratories, Livermore, CA, USA

CHEMKIN-I (1975-1985)

CHEMKIN-II (1985-1995)

Simulation codes: SENKIN, PSR, PREMIX, SHOCK, EQLIB

+ utility programs, data bases

FORTTRAN codes, controlled by the input files

Kee R. J., Rupley F. M., Miller J. A.  
 CHEMKIN-II: A FORTRAN *Chemical Kinetics Package*  
*for the Analysis of Gas-Phase Chemical Kinetics*  
 SANDIA report No. SAND79-8009B

AnSys <https://www.ansys.com/> (formerly ReactionDesign)

Commercial codes; source code is not provided

Chemkin 3.x,

Graphical User Interface (GUI) to CHEMKIN-II

Chemkin 4.x

really new solvers, graphical interface, versatile

Chemkin Pro

Chemkin + additional utility codes (e.g. pathway plotting)

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## CHEMKIN simulation codes

<https://www.ansys.com/>

CHEMKIN → CHEMKIN -II → CHEMKIN 3 → CHEMKIN 4 → CHEMKIN PRO

CHEMKIN (1975– )

classified code

CHEMKIN-II (1986– )

classified code, then freeware

since CHEMKIN 3 (1996– )

commercial code (now: Ansys)

### CHEMKIN-II simulation codes:

SENKIN

spatially homogeneous reactions

PREMIX

laminar premixed flames

SHOCK

shock tube simulations

PSR

perfectly stirred reactor simulations

### Options of SENKIN:

adiabatic system, constant  $p$  pressure

adiabatic system, constant  $V$  volume

adiabatic system,  $V(t)$  function

closed system, constant  $p$ ,  $T$

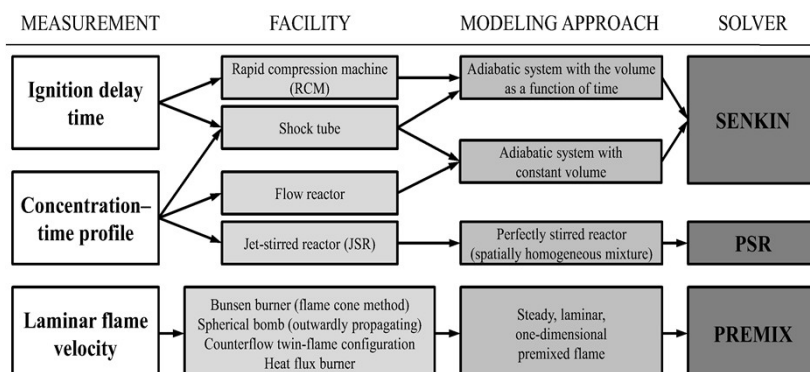
closed system, constant  $V$ ,  $T$

closed system,  $p(t)$  and  $T(t)$  function

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## CHEMKIN-II simulation codes



Relation between the

- measured quantity
- experimental setup
- modelling approach
- the corresponding CHEMKIN-II simulation code

C. Olm, I. Gy. Zsély, R. Pálvölgyi, T. Varga, T. Nagy, H. J. Curran, T. Turányi:  
Comparison of the performance of several recent hydrogen combustion mechanisms.  
*Combust. Flame*, **161**, 2219-2234 (2014).

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## CHEMKIN format of mechanisms

```

ELEMENTS H O N AR END
SPECIES
H2 O2 H2O H2O2 H O OH HO2 N2 AR
END
THERMO ALL
300.000 1000.000 5000.000
H2      H 2 0 0 OG 300.00 5000.00 1000.00 0 1
2.99142300E+00 7.00064400E-04 5.63382900E-08 9.23157800E-12 1.58275200E-15 2
-8.35034000E+02 -1.35511000E+00 3.29812400E+00 8.24944200E-04 8.14301500E-07 3
-9.47543400E-11 4.13487200E-13 1.01252100E+03 3.29409400E+00 4
O2      O 2 0 0 OG 300.00 5000.00 1000.00 0 1
3.69757800E+00 6.13519700E-04 1.25884200E-07 1.77528100E-11 1.13643500E-15 2
-1.23393000E+03 3.18916600E+00 3.21293600E+00 1.12748600E-03 5.75615000E-07 3
1.31287700E-09 8.76855400E-13 1.00524900E+03 6.03473800E+00 4
H2O     H 2 O 1 0 OG 300.00 5000.00 1000.00 0 1
2.67214600E+00 3.05629300E-03 8.73026000E-07 1.20099600E-10 6.39161800E-15 2
-2.989921E+02 6.968581E-01 3.05629300E-03 8.73026000E-07 1.20099600E-10 3
H2O2    H 2 O 2 0 OG 300.00 5000.00 1000.00 0 1
4.573167E+00 1.800690E-01 4.573167E+00 1.800690E-01 4.573167E+00 3
-4.625800E+00 1.800690E-01 4.573167E+00 1.800690E-01 4.573167E+00 3
H       H 1 0 0 0 OG 300.00 5000.00 1000.00 0 1
2.50000000E+00 0.00000000E+00 0.00000000E+00 0.00000000E+00 0.00000000E+00 2
2.54716300E+04 4.60117600E-01 2.50000000E+00 0.00000000E+00 0.00000000E+00 3
0.00000000E+00 0.00000000E+00 2.54716300E+04 4.60117600E-01 4
...

```

for each species, the description of the temperature dependence of  $H$ ,  $S$  and  $c_p$   
NASA polynomials:  $2 \times 7$  parameters

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## CHEMKIN format of mechanisms

```

REACTIONS  MOLES  KJ/DOLES/MOLE
H2+O      => OH+H      5.120E+04  2.67  26.27
OH+H      => H2+O      3.534E+04  2.62  18.95
H2+OH     => H2O+H     1.020E+08  1.60
H2O+H     => H2+OH     4.520E+08  1.60
O2+H+M    => HO2+M     2.100E+18  -.80  .00
N2/0.67/ O2/0.4/ H2O/0./ AR/0.28/
HO2+M     => O2+H+M     1.155E+20  -1.26  211.41
HO2+H2O   => O2+H+H2O   3.801E+17  -.46  202.68
O2+H      => OH+O      9.756E+13  .00  62.11
OH+O      => O2+H      1.450E+13  .00  2.94
H2O2+O    => OH+HO2    6.620E+11  .00  16.63
OH+HO2    => H2O2+O    4.073E+08  .72  77.51
H2O2+OH   => H2O+HO2    7.830E+12  .00  5.57
H2O+HO2   => H2O2+OH    4.744E+11  .45  140.59
H2O2(+M)  => 2OH(+M)    3.000E+14  .00  202.87
N2/0.4/ O2/0.4/ H2O/0.5/ AR/0.35/
LOW / 3.000E+17 .00 190.40 /
TROE / 1.0000 1.00 1.00 1040.00 /
2OH(+M)   => H2O2(+M)   7.230E+13  -.37  .00
N2/0.4/ O2/0.4/ H2O/0.5/ AR/0.35/
LOW / 5.530E+10 -.76 .00 /
TROE / 1.0000 1.00 1.00 1040.00 /
...
END

```

Arrhenius parameters  $A$ ,  $n$ ,  $E$

3<sup>rd</sup> body collision efficiencies

Arrhenius parameters of  $k_0$

Troe-parameters for the description of  $p$ -dependence

## Alternatives to CHEMKIN

Cantera [www.cantera.org](http://www.cantera.org)

Open source code, available from SourceForge.net  
chemical equilibrium, homogeneous and heterogeneous kinetics  
reactor networks, 1D flames

Kintecus [www.kintecus.com](http://www.kintecus.com)

Excel workbook; free for academic use  
Simulation of combustion, atmospheric chemical and biological systems

COSILAB [www.softpredict.com](http://www.softpredict.com)

commercial combustion simulation and mechanism analysis code

- visualization of reaction pathways
- reduction of kinetic mechanisms
- simulation of reactor networks
- two-dimensional reactors and flames
- spray and dust flames

## Alternatives to CHEMKIN 2

**OpenSmoke** (Milano; <http://www.opensmoke.polimi.it/>)

freely available program

numerical modelling of laminar reacting flows

built on the OpenFOAM framework

homogeneous reactions, heterogeneous reactions on catalytic surfaces

**FlameMaster** (Aachen; <http://www.itv.rwthachen.de/downloads/flamemaster/>)

free for academic use

- homogeneous reactor and perfectly stirred reactor calculations
- freely propagating premixed flames
- steady counter-flow diffusion flames

**Chem1D** (Eindhoven; <https://www.tue.nl/>)

flame simulations with both detailed and few-step mechanisms

**laminar flames:**

adiabatic, burner stabilized, ceramic burner stabilized and counterflow flames

**special effects in laminar flames:**

simulation of stretch, curvature, gas radiation

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## SBML

**SBML: Systems Biology Markup Language** <http://sbml.org/>

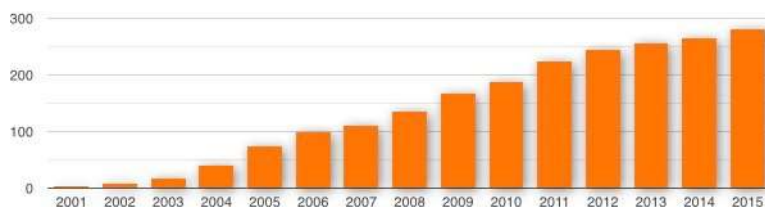
SBML model definition format was created

to promote the exchange of systems biology models

(similar to the role of CHEMKIN format in gas kinetics)

281 SBML-compatible software packages are available (January 2016)

The list of these simulation codes can be looked at <http://sbml.org/>



Increase of the number of SBML-based computer codes  
(these include both academic and commercial codes)

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## Copasi

**COPASI (COmplex PAtchway Simulator)**

<http://copasi.org/>

**Simulation and analysis of biochemical network models.**

Free, support, but source code is not provided.

Homogeneous kinetic systems in interacting compartments

Import and export of models in the SBML format (levels 1 to 3).

Export of models in many format (XPP, C code, Latex).

- ODE-based and stochastic simulations
- stoichiometric analysis of the reaction networks
- optimization of models; parameter estimation
- local sensitivity analysis.
- time scale separation analysis
- characterization of non-linear dynamics properties (oscillations and chaos)

S. Hoops, S. Sahle, R. Gauges, C. Lee, J. Pahle, N. Simus, M. Singhal, L. Xu, P. Mendes, U. Kummer:  
COPASI — a COmplex PAtchway Simulator. *Bioinformatics* **22**, 3067-3074 (2006)

## Global uncertainty analysis codes

**GUI-HDMR** <http://www.gui-hdmr.de>

The GUI-HDMR software is based on the RS-HDMR approach, where all component functions are approximated by orthonormal polynomials using random (or quasi-random) samples. Calculation of up to second-order global sensitivity indices based on user supplied sets of input/output data. The component functions are approximated by up to 10th order orthonormal polynomials.

T. Ziehn, A. S. Tomlin: GUI-HDMR - A software tool for global sensitivity analysis of complex models  
*Environmental Modelling & Software*, **24**, 775-785 (2009)

**SimLab** <https://ec.europa.eu/jrc/en/samo/simlab>

Developed at the EC Joint Research Centre (EC-JRC) in Ispra, Italy.

Versions up to 2.2: GUI based nice education tool

- (1) generation of random or quasi-random parameter sets
- (2) running the models (within SimLab or externally)
- (3) processing of the simulation results (FAST, Morris' and Sobol methods)  
visualisation of the outcome of uncertainty/sensitivity analyses.

SimLab versions from 3.0:

subroutine can be called from Fortran, Python, C++, or Matlab

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*Thank you for  
your attention!*